

# Optimal Idle Speed Control of a Light Duty Turbodiesel Engine With the Aim of Minimizing Fuel Consumption

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## ABSTRACT

Idle Control of Internal Combustion Engines (ICEs) is an important mode of Engine Management Systems (EMS) due to its effects on Fuel Consumption (FC) and pollutions produced in urban traffics. In this paper an optimal controller is used to control the idle speed with respect to minimization of FC in transient situations. In order to design an optimal controller a state space representation of engine in demanded. Subspace identification method is used to derive a proper state space model of engine around idle speed state. The required input/output data is generated using a mean value model. A finite time optimal controller is designed with the aim of minimizing both fuel consumption and speed fluctuations. The influence of finite time value on gross fuel consumption is then studied under various weighting factors. It is shown that the fuel consumption is sensitive to the controlling time duration for finite time LQR.

## INTRODUCTION

Increasing demands for more efficient engines and stricter standard limits on exhaust gas pollutions require more accurate control on engine operating parameters. First generations of internal combustion engines used simple mechanical control instruments such as governors to regulate their operational status. Invention of semiconductors which leads to advent of microcontrollers made it possible to implement more complicated control strategies on mechanical systems, one of which is internal combustion engine. On the other hand new engines are provided with more actuators which in turn increase the number of manipulated parameters. These all have made it possible to decrease both pollution and fuel consumption of engines.

New generation of diesel engines are provided with EMS which controls the injection of fuel, boost pressure and many

other operational parameters. Automotive Idle Speed Controller (ISC) is an important function in engine control field. Engine high nonlinearities in low speeds makes designing of this controller complicated. About 30% of FC during a city driving cycle is spent at idle mode [1]. ISC should be able to keep engine speed in a narrow band close to designed idle speed while exerting external load such as A/C load, alternator load and steering hydraulic pump load. ISC should maintain engine speed in a limited range; lowering speed would cause instability in engine operation while increasing speed from desired speed would increase FC.

A complete review on ISC has been done by Zhengmao [2]. Different methods of modeling, identification and design of ISC have been reviewed in his paper. Many control methods have been used to control idle speed. The first generation of diesel engines used simple mechanical controller mechanisms named governor to regulate their speed. Nowadays with the aid of microcontrollers PID controllers are used due to their robustness and simplicity. However more complex control methods such as adaptive control, optimal control and robust control have been investigated to regulate engine speed in idle mode, most of them were implemented on spark ignition engines. [2] Discrete time control has been used to control a turbocharged diesel engine. In this case the discrete time controller is designed using reference governor for the ISC system. [4] Also an adaptive control algorithm has been used to control a heavy duty diesel engine [5]. Javiar and et.al. used an automatic tuning method for calibrating of a PID controller to increase the performance of a PID base ISC controller for a diesel engine [6]. In their research they used a close-loop identification method to estimate the parameters of engine based on a first order system with time delay and used the estimated parameters to tune the PID controllers. Mills used a multivariable LQG control algorithm for regulating the idle speed of a diesel engine, in his research a nonlinear engine

model was used to design and test the controller [7]. Also Han and et.al. used a non-linear model of a diesel engine and linearized it around idle speed to design an optimal controller for regulating the engine speed. They estimated the model parameters using nonlinear identification method based on numerous tests done on the engine. They could successfully control the engine [8].

In this paper a linear state space identification method is used based on input/output data which are generated from a mean value model of a turbocharged engine. 4 states are used to develop the model. A finite time LQR controller is used then to control the engine speed with aiming at minimizing the fuel economy.

## DIESEL ENGINE DYNAMIC MODELING

In order to identify the engine dynamics a comprehensive model of engine is needed. The model should also be accurate enough to predict engine behavior under operational conditions. Many researches have been done to simulate the engine dynamic behavior. In order to simulate the dynamic performance of engine, Mean Value Model (MVM) is utilized. To model the engine performance required information such as turbocharger maps, torque generation efficiency, geometric and dynamic characteristics of engine are collected from the test results obtained by Hendricks and et al. [9]. The model contains inlet and exhaust manifolds, turbocharger, torque generation, internal friction and crank shaft dynamic sub models. Figure 1 illustrates the numbering sequence of engine. A brief description of engine modeling procedure is mentioned in following paragraphs. The variables in following equations are introduced in definition section of paper.

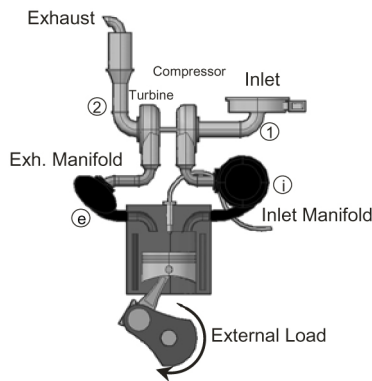


Fig. 1. Schematics of engine and numbering sequence

The test data used in this paper is obtained from the experimental data published by Hendricks and et.al, the engine properties are as follows [9]:

Table 1. Engine Properties

Cylinder Bore	76/5 mm
Stroke	86/4 mm
Displacement volume	1588 CC
Compression ratio	23:1
Max. Power	50 kW @ 4000 rpm
Engine rotational part inertia	0/58 kg.m <sup>2</sup>
Turbine diameter	22 mm
Turbine shaft inertia	0/9 × 10 <sup>-5</sup> kg.m <sup>2</sup>

## TURBOCHARGER MODEL

In order to compress the inlet air, mechanical energy is fed to compressor; the required mechanical torque is calculated using the following formula:

$$T_c = \frac{\dot{m}_c C_{pa} T_1}{\eta_c \omega_{tc}} \left[ \left( \frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \quad (1)$$

Compressor model is able to predict the required torque, flow rate and temperature of inlet air. The performance maps of compressor are usually published by turbocharger manufacturer and are used as a 2D lookup table. These maps are applied in the model using the Hendricks and et al. test data [9]. The turbine generated torque is also calculated as follows:

$$T_t = \frac{\dot{m}_t C_{p,e} T_3 \eta_t}{\omega_{tc}} \left[ 1 - \left( \frac{P_4}{P_3} \right)^{\frac{\gamma_e-1}{\gamma_e}} \right] \quad (2)$$

Exhaust gas mass flow rate through the turbine is a function of turbine pressure ratio and turbine shaft speed. Also the turbine efficiency is a function of air flow Mach number and turbine shaft speed. These functions are also used in the model as 2D lookup tables. Furthermore, the dynamic model of turbocharger shaft is used to interconnect the turbine sub model and compressor and is formulated using following equation:

$$T_t - T_c = I_{tc} \dot{\omega}_{tc} \quad (3)$$

Where  $I_{tc}$  is the rotational inertia of interconnecting shaft.

## INLET AND EXHAUST MANIFOLDS MODELS

In turbocharged engines, the manifolds are intermediate volumes placed between compressor and inlet ports or turbine and exhaust ports. The air flow of turbine and compressor has been calculated before. The engine air flow rate is calculated using the volumetric efficiency as follows:

$$\dot{m}_{en}(t) = \rho_2(t) \eta_v(P_2, \omega_{en}) \frac{V_d}{N} \frac{\omega_e(t)}{2\pi} \quad (4)$$

The volumetric efficiency is a function of inlet manifold pressure and engine RPM.

$$\eta_v = \eta_{v,p}(P_2) \eta_{v,\omega}(\omega) \quad (5)$$

The results of a test are considered to investigate the effects of engine speed on volumetric efficiency [9]. The inlet manifold pressure plays an important role on volumetric efficiency; there are many models which predict the volumetric efficiency as a function of inlet pressure. Inlet manifold pressure is calculated using the differential equation 6 which includes the compressor air flow rate and engine suction flow rate [10]:

$$\dot{P}_2 + \frac{\eta_v V_d N}{120 V_{im}} P_2 = \dot{m}_c \frac{RT_2}{V_{im}} \quad (6)$$

Also temperature and pressure in formula 6 are calculated using appropriate thermodynamic relations.

## TORQUE GENERATION, INTERNAL FRICTION AND CRANKSHAFT DYNAMIC MODELS

In order to model the engine accurately, the thermal efficiency of engine should be available. Engine torque generation depends on some of the engine operational parameters. It is shown that the diesel engine thermal efficiency is mainly a function of three major parameters:

$$\eta_{ind} = f(N, \lambda, \zeta) \quad , \quad \frac{1}{\lambda} = \phi = \frac{(F/A)_{actual}}{f_s} \quad (7)$$

The way which thermal efficiency is related to engine speed and equivalence ratio is derived using the experimental data. This function is applied into the model as a 2D lookup table. The effect of injection timing  $\zeta$  on torque generation is modeled as a second order function [11]. The result torque is calculated using energy equations. The generated torque, external load and internal friction torque together accelerate or decelerate

the crankshaft. The following dynamic equation is used to calculate the engine speed.

$$T_{ind} - T_f - T_l = I_{cr} \cdot \dot{\omega}_{cr} \quad (8)$$

In the above formula  $T_f$  represents the internal friction torque of engine moving parts and also pumping losses of engine. The pumping loss is calculated considering the difference between exhaust gas pressure and inlet pressure while the friction part is calculated as a function of both temperature and speed of engine [12].

## MODEL VALIDATION

After calibrating of the model using steady state responses, it was tested by a step unloading of 10 N.m at 10th sec and subsequent loading of 10 N.m in 30th sec.

As figure 2 illustrates, the engine speed increases due to unloading in 10th sec and decreases to initial speed again. The trend of variations shows good similarity between experimental results and model ones.

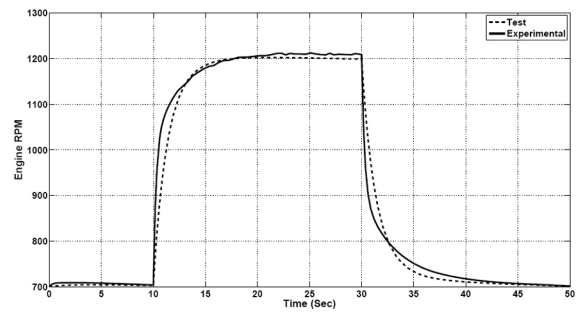


Fig. 2. Comparison of speed variation in model and experiment due to a step unloading and loading of 10 N.m

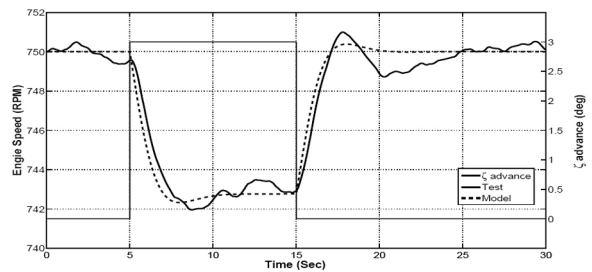
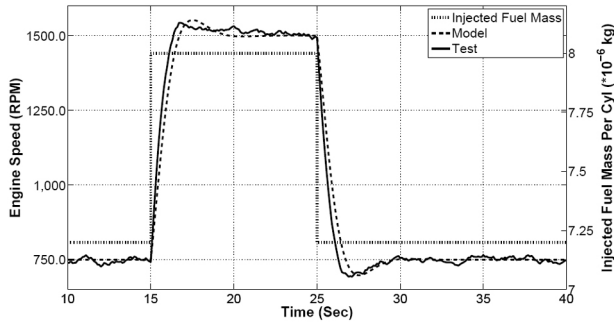


Fig. 3. Comparison of speed variation in model and experiment due to a step change in injection angle

An important manipulated variable is Injection timing  $\zeta$  which will be discussed later. It will cause engine speed to vary. A test is done on the engine to see how the engine would response to  $\zeta$  variation. In 5th second the injection angle is retarded 3 crank angles from MBT and is returned to MBT condition in

15th second. The low domain variations in speed are results of cycle by cycle variations in torque generation which are now more apparent. It also shows that the injection timing maybe used to compensate for low speed disturbances. However using this manipulated variable will decrease the fuel economy of engine while running in idle mode.



**Fig. 4. Comparison of speed variation in model and experiment due to a step change in injected fuel mass**

The other parameter which severely affects the engine speed is mass of fuel injected per cycle for every cylinder. The comparison between the model and experimental data show that model is able to predict the engine behavior accurately enough to be used for designing the controller.

## DIESEL ENGINE IDENTIFICATION

### SUBSPACE SYSTEM IDENTIFICATION

System identification is a method to derive a mathematical model for dynamic systems based on I/O data. Different methods of dynamic system identification are classified to linear and nonlinear methods. Recently fuzzy and neural networks have also been employed to identify dynamic systems [13, 14]. In this paper a linear approach is utilized to identify a state space model based on subspace method. Subspace identification is an efficient computational method to derive a state space model out of I/O data [15]. Below a full description of subspace identification method is considered regarding to Keyvaani and et al. paper on subspace identification approach [16]:

Subspace identification is a method for identification of multivariable LTI systems. This method provides a good alternative to classical nonlinear optimization based prediction error methods. Subspace identification methods for LTI systems can basically be classified into two different groups: The first group consists of the methods that aim at recovering the column space of extended observability matrix and use the shift-invariant structure of this matrix to estimate the matrices A and C; this group consists of so called MOESP methods. The second method aim at approximating the state sequence of the system and use this approximate state in a second step to estimate the

system matrices; the method that constitute this group are the N4SID method, the CVA methods and the orthogonal decomposition method. The acronym N4SID stands for “Numerical algorithms for Subspace State Space System Identification”. The algorithm determines the order of the system directly from the singular value decomposition of the oblique projection. The interested reader are referred to [14, 15] to gain detail information about this identification method.

## SYSTEM IDENTIFICATION USING MATLAB

In this paper Matlab® Identification Toolbox is used to identify the linear model based of N4SID method. As discussed earlier in modeling section, turbocharged diesel engine has four main dynamics processes related to inlet manifold, exhaust manifold, turbocharger inertia and crankshaft inertia. The corresponding states are  $P_p$ ,  $P_o$ ,  $N$  and  $N_{tc}$  respectively, where  $P_i = P_2$  and  $P_e = P_3$ . The process to identify the engine state space model is done in two main steps:

### 1. Identification of an intermediate state space model

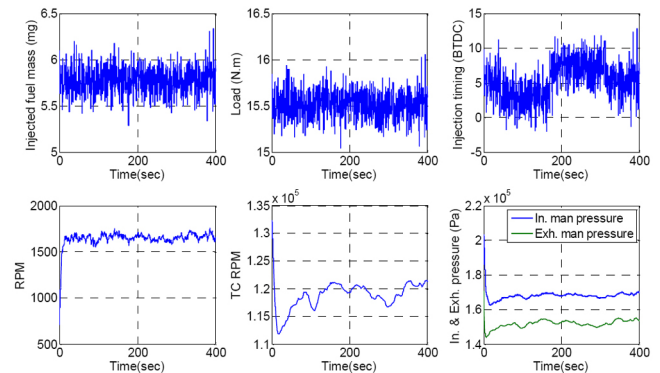
with 3 inputs of  $u = [T_l \quad m_f \quad \xi]^T$  and 4 outputs of

$y = [N \quad N_{tc} \quad P_i \quad P_o]^T$  based on I/O data. The order of the system is obtained by the singular value decomposition method.

### 2. Performing a linear transformation to transform the intermediate model to desired model with states of

$$x = [N \quad N_{tc} \quad P_i \quad P_o]^T$$

I/O data used in identification is generated from the MVM developed before. The generated data are selected so that they are able to take influences of all the inputs into account. Random white noise with appropriate intensity is used to generate the demanded data. In identification procedure, 8 distinct generated data sets are used simultaneously to model engine behavior accurately, one of which is illustrated below:



**Fig. 5. A set of input-output data**

Using the N4SID scheme, a discrete state space equation results in following form with sampling time of  $T = 0.1 \text{ Sec}$  :

$$\begin{cases} x'(t+T)_{8 \times 1} = A'_{4 \times 4} x'(t) + B'_{4 \times 3} u(t)_{3 \times 1} \\ y(t)_{4 \times 1} = C'_{4 \times 8} x'(t) + D'_{4 \times 3} u(t), D' = 0 \end{cases} \quad (9)$$

In which  $u = [T_l \quad m_f \quad \xi]^T$  and  $y = [N \quad N_{ic} \quad P_i \quad P_o]^T$ . This state space equation has non-meaningful states due to subspace identification. A linear transformation is applied to transform the equation 16 to a system with meaningful states as follow:

$$\begin{cases} y(t+T)_{4 \times 1} = A_{d4 \times 4} y(t) + B_{d4 \times 3} u(t)_{3 \times 1} \\ N(t)_{4 \times 1} = C_{4 \times 4} y(t) \end{cases} \quad (10)$$

Since  $D' = 0$  in equation 16, state equation and output equation can be merged. Consequently A and B matrices are computed:  $A_d = C'A'C^{-1}$ ,  $B_d = C'B'$  furthermore output is simply the first state of system and also  $D = 0$ . In order to derive a continuous state space model, the following matrix functions are used:

$$\begin{aligned} A_d &= e^{AT} \\ B_d &= (e^{AT} - I)A^{-1}B \Rightarrow B = A(A_d - I)^{-1}B_d \end{aligned} \quad (11)$$

In which  $A_d$  and  $B_d$  are state and input matrices of discrete state space system respectively and  $T$  is sampling time of discrete system. In order to describe the engine state space in more meaningful manner, the input signals are expanded to disturbance signal and real input signals; load is really a disturbance while injected mass and injection timing are two real inputs to engine. So equation 9 will alter to following form:

$$\begin{cases} y(t+T) = Ay(t) + Bu(t) = Ay(t) + B_u u_{new}(t) + Ev(t) \\ N(t) = Cy(t) \end{cases} \quad (12)$$

Where  $v(t)$  is disturbance (load) and  $u_{new}(t)$  is input vector which contains injection mass and injection timing. The matrices in equation 12 will calculated to be:

$$A = \begin{bmatrix} -0.3679 & 0.0042 & -0.0043 & 0.0008 \\ -2.9647 & 0.0524 & -0.1661 & 0.1534 \\ -0.9883 & 0.0456 & -0.2064 & 0.2115 \\ 7.0695 & 0.0073 & 0.0369 & -0.1088 \end{bmatrix}$$

$$B_u = \begin{bmatrix} 272.6 & -9.3 \\ -241.8 & -128 \\ -2757.1 & -94.4 \\ -830.6 & 157.7 \end{bmatrix}, E = \begin{bmatrix} -52.8 \\ 330.5 \\ 957.9 \\ 109.5 \end{bmatrix}$$

$$C = [I \quad 0 \quad 0 \quad 0]$$

Where  $A$  is state dynamic matrix,  $B_u$  is input matrix,  $E$  is disturbance matrix and  $C$  is output matrix.

## STATE SPACE MODEL VALIDATION

The state space model is verified by appropriate stimulus, a test procedures is done to verify the state space model. The stimuli and result of test are illustrated in figures 6 and 7. The results show an adequate agreement between state space and nonlinear model. The test results show that engine speed prediction have a RMS error of 3.46%, 6.57%, 3.74% and 2.65% for engine RPM, turbocharger RPM, inlet and exhaust pressure respectively for step sequence.

## CONTROLLER DESIGN

### LQR FINITE TIME CONTROLLER

The optimal control is best suited for cases which convert energy to other forms, the major effect of optimal control is its effect on systems in transient behavior. Usually optimal control compromises between output performance and effort energy. The weighting factors are used to balance between input values and output performance. In optimization of system can be considered for a finite time or and infinite time span. The finite time LQR method is an optimal controlling approach based on minimization of a performance index in a finite time as follows, where  $u(t)$  is the controlling effort and  $r$  is the reference value of states.

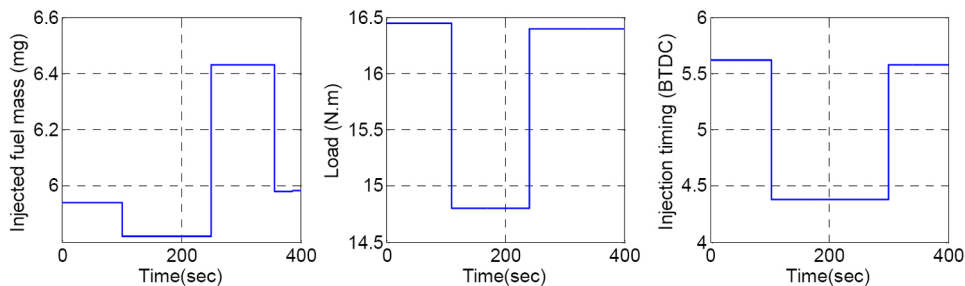


Fig. 6. Step sequences stimuli for verification test

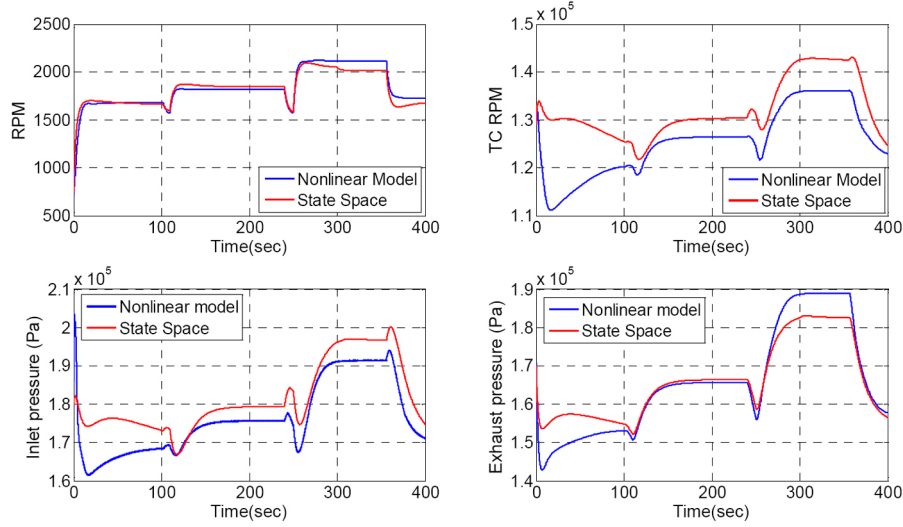


Fig. 7. Result of verification for step sequences input

$$J = \frac{1}{2} [x(t_f) - r]^T H [x(t_f) - r] + \frac{1}{2} \int_0^{t_f} \{ [x(t) - r]^T Q [x(t) - r] + u^T(t) R u(t) \} dt \quad (13)$$

The main problem is to find a control effort  $u(t)$  in such a way to minimize the above performance index. Based on Hamiltonian method the appropriate controlling effort is calculated as follow:

$$u(t) = -R^{-1} B_u^T K(t) x(t) - R^{-1} B_u^T s(t) \quad (14)$$

In which  $K(t)$  and  $s(t)$  are simply the solution of following differential equations:

$$\begin{aligned} \dot{K}(t) &= -K(t)A - A^T K(t) - Q + K(t)B_u R^{-1} B_u^T K(t) \\ K(t_f) &= H \end{aligned} \quad (15)$$

$$\begin{aligned} \dot{s}(t) &= -[A^T - K(t)B_u R^{-1} B_u^T] s(t) + Qr \\ s(t_f) &= -Hr \end{aligned} \quad (16)$$

Matlab® is used to solve the above differential equations, depend on selection of  $Q$ ,  $H$  and  $R$  different controlling scenarios are resulted, some of which are illustrated and discussed follow. Different loading sequences are tested to check the controller performance. On the other hand different time spans are simulated to check the effect of finite time on engine fuel consumption.

Since only the engine speed is to be regulated in 750 RPM,  $Q$  and  $H$  matrices takes into account only the first state. The weighting and set point matrices are defined as follows:

$$Q = \begin{bmatrix} q_{rpm} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}, H = \begin{bmatrix} h_{rpm} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}, R = \begin{bmatrix} r_f & 0 \\ 0 & r_T \end{bmatrix}, r = \begin{bmatrix} 750 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (17)$$

The system response for sinusoidal external loads is considered follow, engine speed, TC speed, inlet and exhaust pressures and corresponding injection fuel mass and injection timing values are illustrated in figures 9 and 10 for different weighting combinations. Also the external load is illustrated in figure 8.

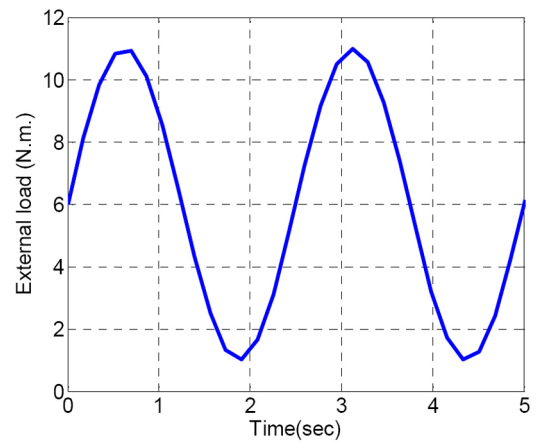
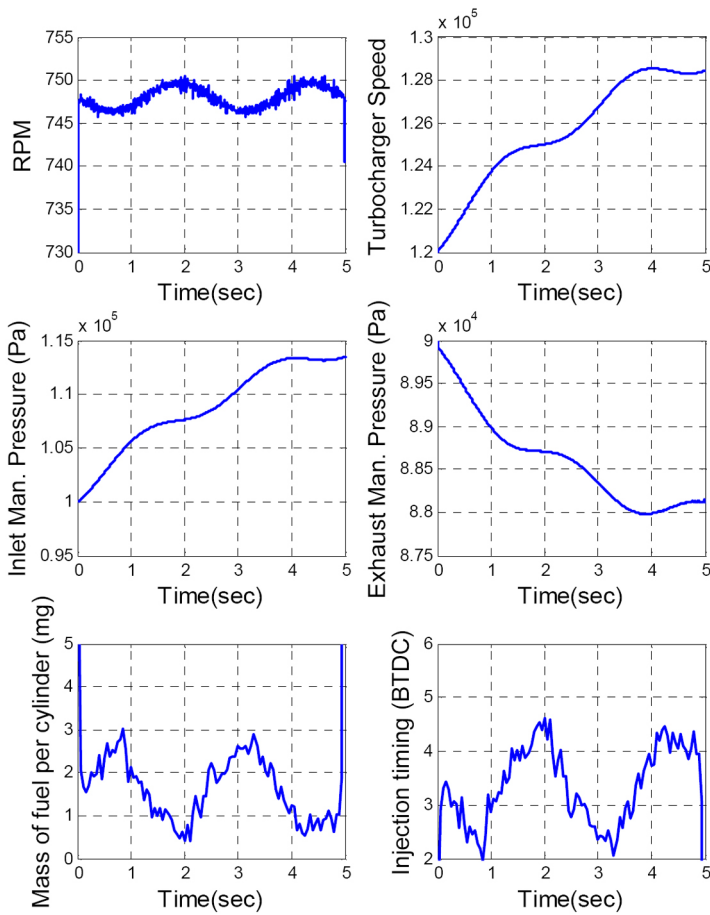
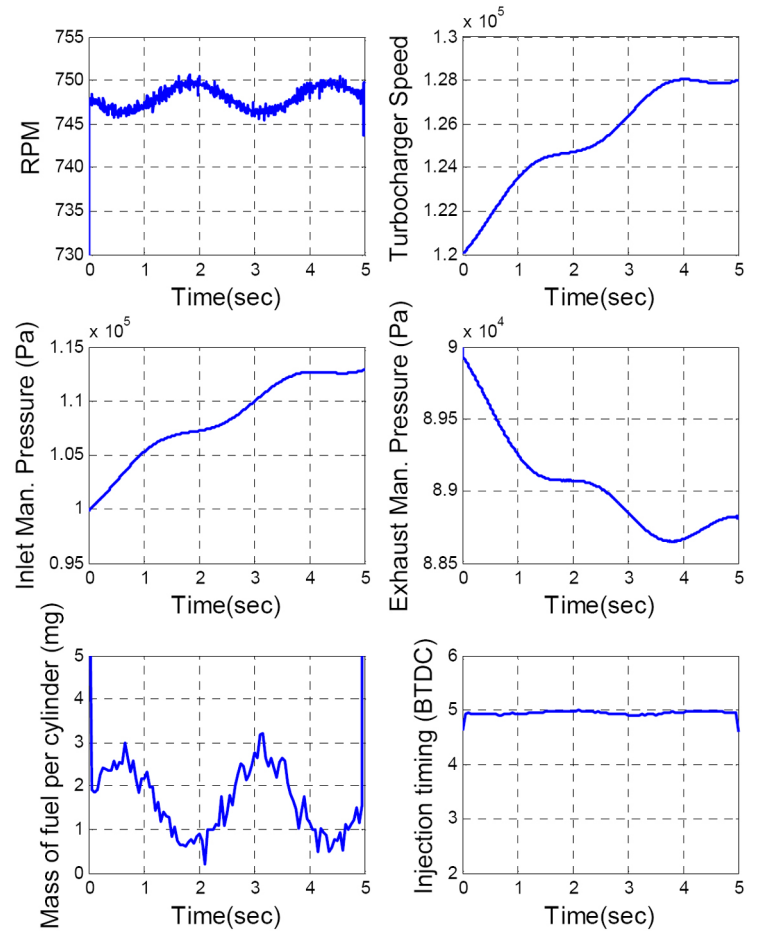


Fig. 8. The external sinusoidal load



**Fig. 9. The controlled states and corresponding optimal inputs for  $q_{rpm} = 1$ ,  $h_{rpm} = 6$ ,  $r_f = 3$ ,  $r_{IT} = 0.1$**



**Fig. 10. The controlled states and corresponding optimal inputs for  $q_{rpm} = 1$ ,  $h_{rpm} = 1$ ,  $r_f = 3$ ,  $r_{IT} = 3$**

As illustrated in figures 9 and 10, increasing  $r_{IT}$  will lower the deviation of injection timing, on the other hand varying controller parameter does not affect inlet manifold pressure and TC speed, but it affects exhaust manifold pressure to some extend.

## SENSITIVITY ANALYSIS

After designing the controller, the controller parameter should be tuned regard design demands. The parameters to tune are weighting parameters in equation 17, e.g.  $q_{rpm}$ ,  $h_{rpm}$ ,  $r_f$ ,  $r_{IT}$  which stand for speed transient, speed target, fuel injection in transient and injection timing in transient respectively. On the other hand the other important parameter which should be taken into account is the value of final time  $t_f$  in equation 13 which stands for the value of control time duration. The  $q_{rpm}$ ,  $r_f$ ,  $r_{IT}$  parameters are tuned based on importance of each parameter. Increasing  $r_f$  will decrease fuel consumption while increasing  $q_{rpm}$  decreases the speed fluctuations in expense of fuel economy. Increasing  $r_{IT}$  lowers the deviation of injection

timing relative to optimal injection timing which is turn would decrease fuel consumption.

At last the following value are assigned to weighting factors,  $q_{rpm} = 1$ ,  $r_f = 3$ ,  $r_{IT} = 2$ . The time span for LQR finite time controller and  $h_{rpm}$  are analyzed to find their optimum value based on engine fuel consumption. In order to make an optimum tuning the variation of fuel consumption is plotted versus finite time value for different  $h_{rpm}$  s. A sinusoidal input of 2Hz frequency is used to examine the controller.

As illustrated in figure 11, the effect of  $h_{rpm}$  on fuel consumption is not important for finite time values of more than 5 sec, also it has been shown that the fuel consumption converge to a fix value of 2 mg/cyl for time values of more than 5 sec. It is also obvious that fuel consumption increase with increasing  $h_{rpm}$  in low time spans. It's mostly due to effects of  $h_{rpm}$  on speed regulation. Decreasing  $h_{rpm}$  will increase the settling time. At last  $h_{rpm} = 2$  and  $t_f = 5$  sec is selected due to their optimal effects of fuel consumption.

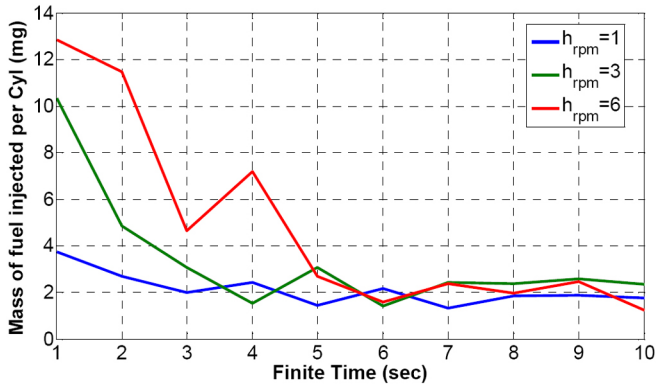


Fig. 11. Controller parameter tuning based on fuel consumption optimization

In order to verify the controller design with the optimal parameters a step load is exerted to engine as follows:

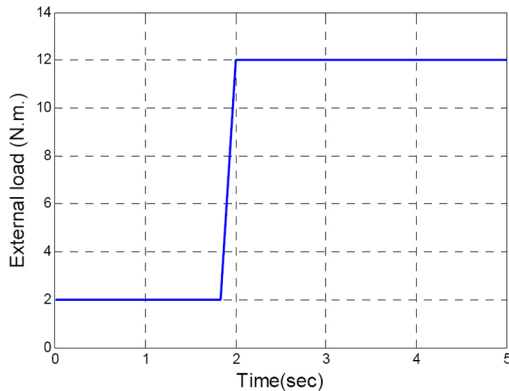


Fig. 12. The external step load

The result of controller is illustrated in figure 13.

## CONCLUSION

A new approach for developing state space representation of engine is used instead of normal linearization methods which needs differentiable equations. The testing procedure for identification procedure is minimized by introduction of a mean value model instead of real engine. A LQR finite controller the applied to the model to regulate the speed of engine to desired idle speed, variation of weighing values are studied, it is apparent that increasing fuel consumption weight result is decreasing fuel consumption while increasing speed variation, on the other hand the final time weighting value has not significant effect on control procedure. Some deviation from desired speed is seen in the controlled value (RPM), it's mostly because the influences of load on system dynamics as seen in Eq. 12. the variation in speed decreases by increasing the RPM weighting value. Also it is shown that  $t_f$  is an effective

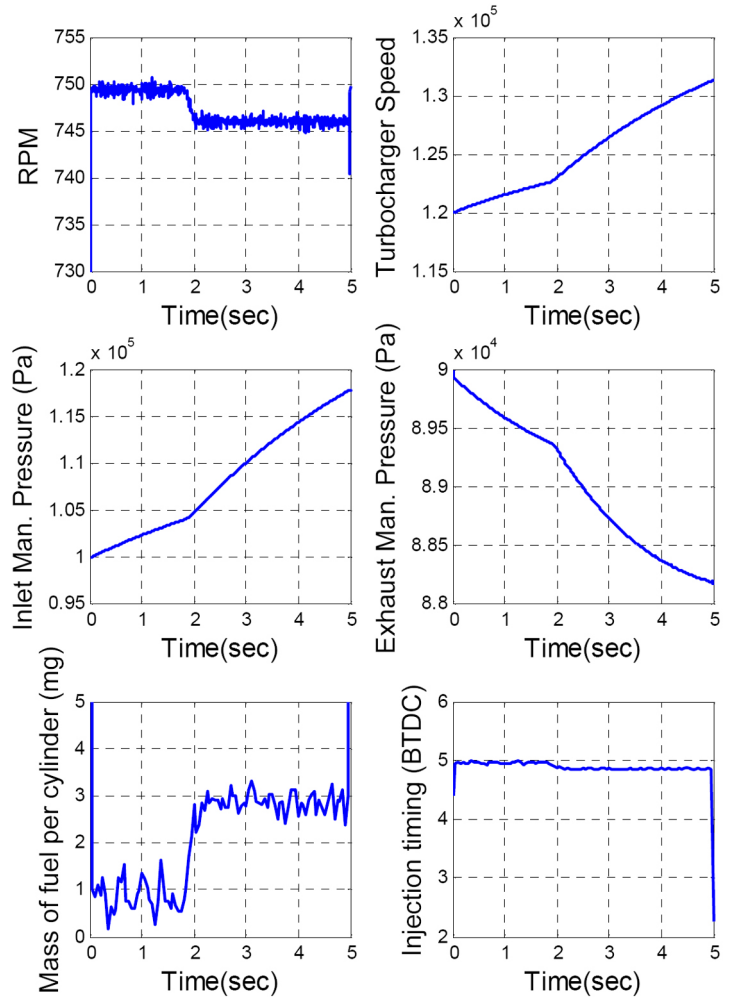


Fig. 13. The controlled states and corresponding optimal inputs for the step load

parameter on fuel consumption (controller target), furthermore the effects of  $h_{rpm}$  on fuel consumption is significant for low  $t_f$  (final control time).

## DEFINITIONS

Notation	Description	unit
$B$	Cylinder bore	$m$
$C_{p,a}$	Heat capacity of inlet air	$kJ/kg.K$
$C_{p,e}$	Heat capacity of exhaust gas	$kJ/kg.K$
$(F/A)_a$	Actual fuel to air ratio	
$f_{mep_f}$	Friction mean effective pressure due to wet friction	$Pa$
$f_s$	Stoichiometric fuel to air ratio	
$h_{rpm}$	Weighting factor for speed regulation	



			<b>Notation</b>	<b>Description</b>	<b>unit</b>
$I_{cr}$	Crankshaft and engine rotating part inertia	$kg.m^2$	$\Gamma_d$	Observability matrix	
$I_{tc}$	Turbocharger shaft and blades rotational inertia	$kg.m^2$	$\Pi_{e,max}$	Maximum ratio of exhaust pressure to inlet	
$\dot{m}_c$	Mass rate of air through compressor	$kg/sec$	$\phi$	Fuel to air equivalence ratio	
$\dot{m}_{en}$	The passing air mass flow rate through engine	$kg/sec$	$\gamma_a$	Air specific heat ratio	
$\dot{m}_{ex}$	Exhaust gas mass flow rate	$kg/sec$	$\gamma_e$	Exhaust gas specific heat ratio	
$m_f$	Mass of injected fuel per cylinder	$mg$	$\eta_c$	Compressor efficiency	
$\dot{m}_t$	Mass rate of gas through turbine	$kg/sec$	$\eta_{ind}$	Engine indicated efficiency	
$N$	Engine speed	$RPM$	$\eta_t$	Turbine efficiency	
$N_{tc}$	Turbocharger speed	$RPM$	$\eta_v$	Volumetric efficiency of engine	
$P_1$	Pressure of air before compressor	$Pa$	$\eta_{v,\omega}$	Volumetric efficiency (speed related part)	
$P_4$	Pressure of exhaust gas after turbine	$Pa$	$\lambda$	Air to fuel equivalence ratio	
$P_e$	Exhaust manifold pressure	$Pa$	$\omega_e$	Engine speed	$Rad/sec$
$P_i$	Inlet manifold pressure	$Pa$	$\omega_{tc}$	Turbocharger speed	$Rad/sec$
$q_{in}$	Combustion specific heat value	$kJ/kg$	$\zeta,$	Injection timing	$BTDC^\circ$
$q_{rpm}$	Weighting factor for speed fluctuations		$\zeta_0$	Injection timing correspond to MBT	$BTDC^\circ$
$r_c$	Compression ratio				
$r_{IT}$	Weighting factor for Injection Timing				
$r_f$	Weighting factor for mass of injected fuel				
$S$	Piston stroke	$m$			
$t_f$	LQR Controlling time duration (finite time LQR)				
$T_1$	Temperature of air before compressor	$K$			
$T_4$	Temperature of exhaust gas after turbine	$K$			
$T_c$	Compressor demanded torque	$N.m$			
$T_f$	Friction torque	$N.m$			
$T_{ind}$	Engine indicated torque	$N.m$			
$T_l$	Load torque	$N.m$			
$T_t$	Turbine generated torque	$N.m$			
$V_c$	Combustion chamber volume	$m^3$			
$V_d$	Engine displacement volume				
$V_{im}$	Inlet manifold volume	$m^3$			

## ABBREVIATIONS

### I/O

Input-Output

### CVA

Canonical Variable Analysis

### EMS

Engine Management System

### FC

Fuel Consumption

### ICE

Internal Combustion Engine

### ISC

Idle Speed Controller

### LQG

Linear Quadratic Gaussians

### LQR

Linear Quadratic Regulators

### LTI

Linear Time Invariant

### MBT

Maximum Brake Torque

## MOESP

Multivariable Output Error State Space

## MVM

Mean Value Model

## N4SID

Numerical algorithms for Subspace State Space  
System Identification

## RMS

Root Mean Square

## SVFC

State Vector Feedback Control

## TC

TurboCharger

## VGT

Variable Geometry Turbine

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